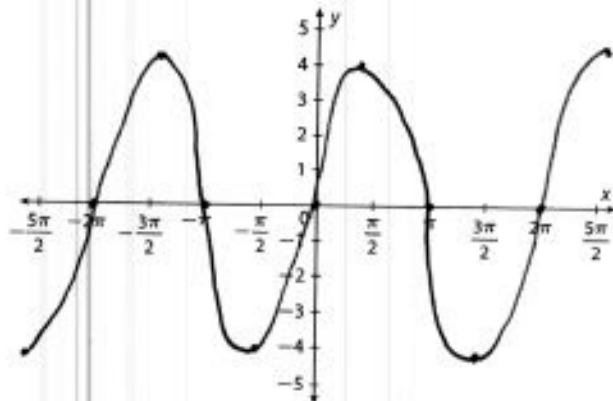


Graphs of Trig Functions

For each trigonometric function, identify the vertical stretch or compression and the horizontal stretch or compression. Then, graph the function and identify its period.

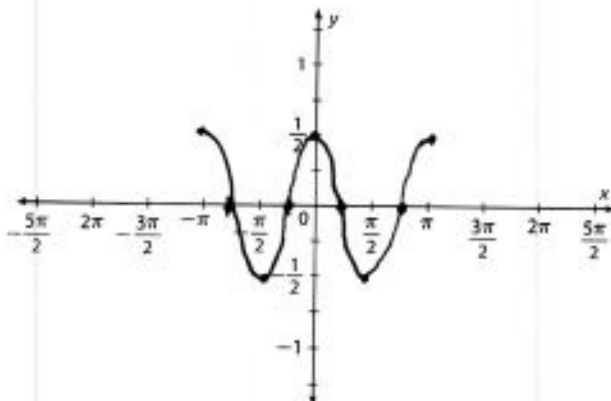
1. $y = 4 \sin x$ V.S. of 4



$p = 2\pi$

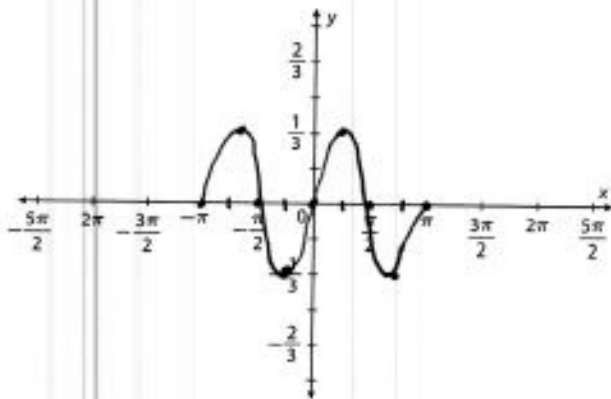
2. $y = \frac{1}{2} \cos 2x$

v. comp. $\frac{1}{2}$
h. stretch 2



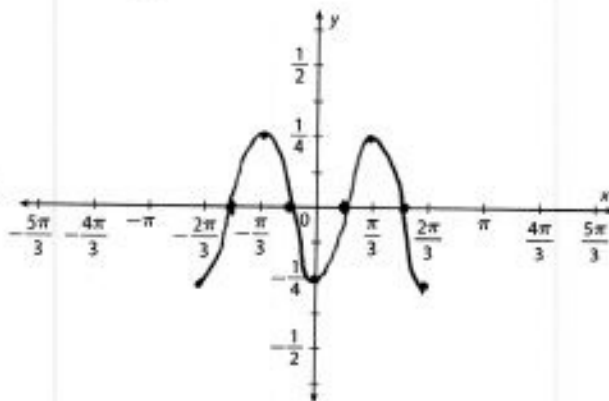
$p = \pi$

5. $y = \frac{1}{3} \sin 2x$ v.s. $\frac{1}{3}$
h.c. 2



per = π

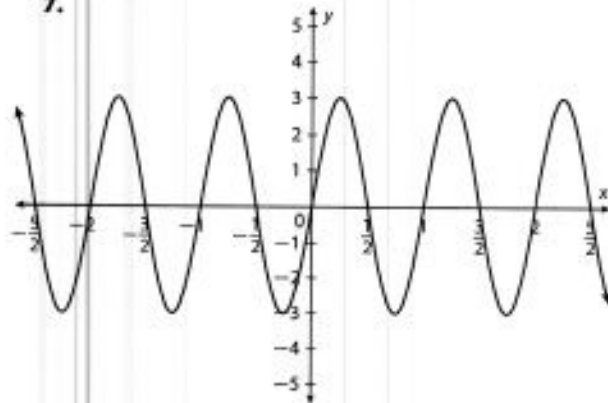
6. $y = -\frac{1}{4} \cos 3x$



per = $\frac{2\pi}{3}$

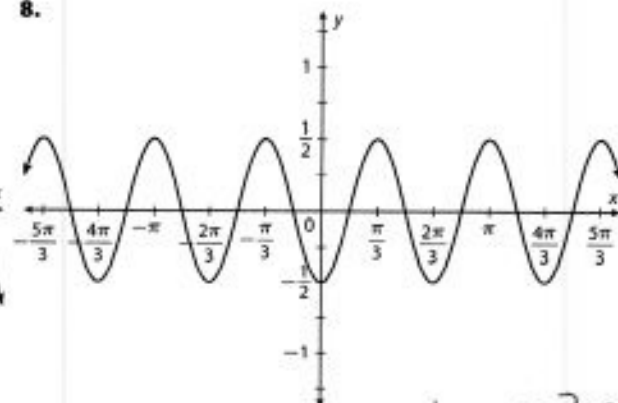
Write an equation for each graph.

*7.



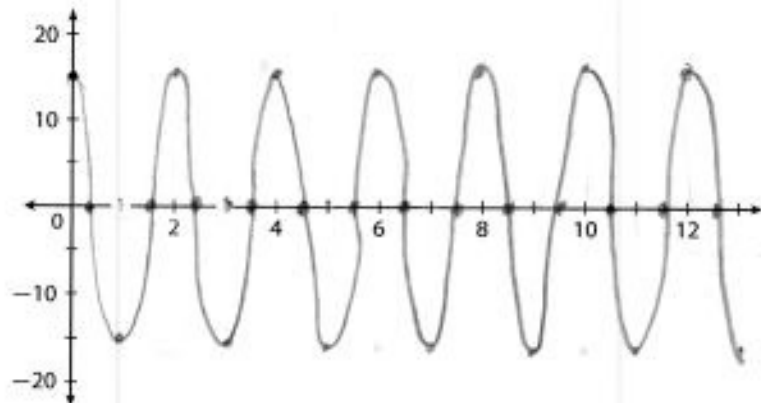
$$f(x) = 3 \sin 2\pi x$$

8.



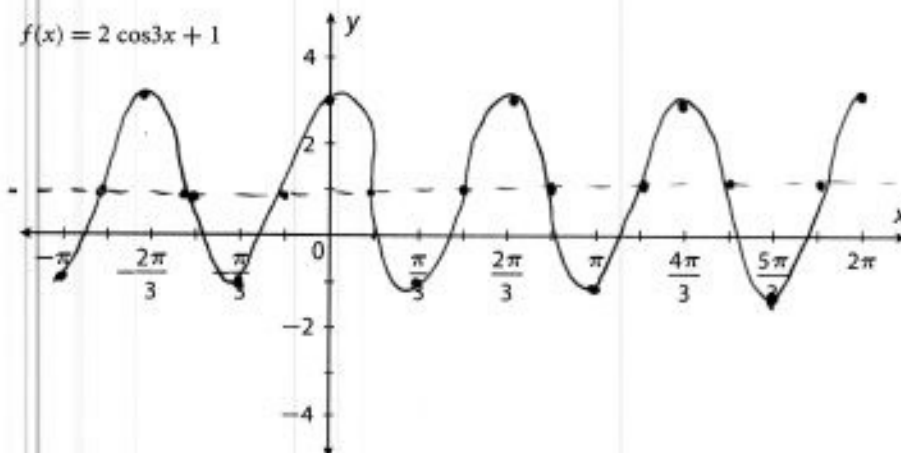
$$f(x) = -\frac{1}{2} \cos 3x$$

- *14. Physics A mass attached to a spring oscillates up and down every 2 seconds. Draw a graph of the vertical displacement of the mass relative to its position at rest if the spring is stretched to a length of 15 cm before the mass is released.



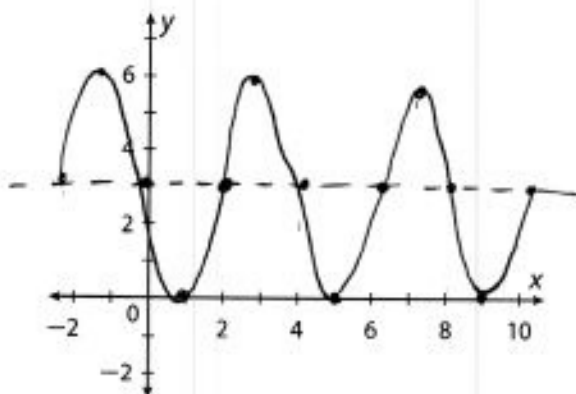
For each function, identify the period and the midline of the graph, and where the graph crosses the midline. For a sine or cosine function, identify the amplitude and the maximum and minimum values and where they occur.

2. $f(x) = 2 \cos 3x + 1$



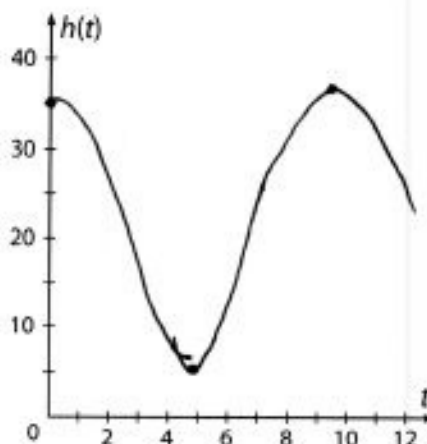
period: $\frac{2\pi}{3}$ midline $\rightarrow y = 1$
 $a = 2$ max: 3 min: -1

4. $f(x) = 3\sin\frac{\pi}{2}(x-2) + 3$



$a=3$
 $per = 2\pi \cdot \frac{2}{\pi} = 4$
 right 2
 up 3
 midline = 3

8. **Historic Technology** Water turns a water wheel at an old mill. The water comes in at the top of the wheel through a wooden chute. The function $h(t) = 15\cos\frac{\pi}{5}t + 20$ models the height h in feet above the stream into which the water empties of a point on the wheel where t is the time in seconds.



Review

Find the following values that satisfy the interval of $0 \leq \theta \leq 2\pi$

1. $\cos\left(\sin^{-1}\frac{\sqrt{3}}{2}\right)$

$\cos(60^\circ)$ or $\cos(120^\circ)$

$\frac{-1}{2}$ or $\frac{1}{2}$

2. $\cot(\sec^{-1}\sqrt{2})$

$\cot(45^\circ)$ or $\cot(315^\circ)$

1 or -1

3. $\csc(\tan^{-1}0)$

$\csc(0)$ or $\csc(180^\circ)$

und or