

Given a polynomial divisor and dividend, use long division to find the quotient and remainder.

1. $(18x^3 - 3x^2 + x - 1) \div (x^2 - 4)$

$$\begin{array}{r} 18x-3 \\ x^2-4 \overline{) 18x^3-3x^2+x-1} \\ \underline{+(-18x^3 \quad +72x)} \\ -3x^2+73x-1 \\ \underline{+ (+3x^2 \quad +12)} \\ 73x-13 \end{array}$$

$$18x-3 + \frac{73x-13}{x^2+4}$$

2. $(6x^4 + x^3 - 9x + 13) \div (x^2 + 8)$

$$\begin{array}{r} 6x^2+x-48 + \frac{-17x+397}{x^2+8} \\ x^2+8 \overline{) 6x^4+x^3+0x^2-9x+13} \\ \underline{-(6x^4 \quad +48x^2)} \\ x^3-48x^2-9x+13 \\ \underline{-(x^3 \quad +8x)} \\ -48x^2-17x+13 \\ \underline{+ (+48x^2 \quad +384)} \\ -17x+397 \end{array}$$

3. $(x^3 + 25x^2 + 100x) \div (x + 20)$

$$\begin{array}{r} x^2+5x \\ x+20 \overline{) x^3+25x^2+100x} \\ \underline{+ (-x^3-20x^2)} \\ 5x^2+100x \\ \underline{-(5x^2+100x)} \\ 0 \end{array}$$

Given a polynomial $p(x)$, use synthetic division to divide by $x - a$ and obtain the quotient and the (nonzero) remainder.

4. $(7x^3 - 4x^2 - 400x - 100) \div (x - 8)$

$$\begin{array}{r|rrrr} 8 & 7 & -4 & -400 & -100 \\ & \downarrow & 56 & 416 & 128 \\ \hline & 7x^2 & +52x & +16 & 28 \end{array}$$

$$7x^2 + 52x + 16 + \frac{28}{x-8}$$

5. $(2.5x^3 + 6x^2 - 5.5x - 10) \div (x + 1)$

$$\begin{array}{r|rrrr} -1 & 2.5 & 6 & -5.5 & -10 \\ & \downarrow & -2.5 & -3.5 & 9 \\ \hline & 2.5x^2 & +3.5x & -9 & -1 \end{array}$$

$$2.5x^2 + 3.5x - 9 + \frac{-1}{x+1}$$

6. $(3x^3 - 11x^2 - 56x - 50) \div (x + 4)$

$$\begin{array}{r} -4 \overline{) 3 \quad -11 \quad -56 \quad -50} \\ \underline{ 3 \quad -12 \quad 92 \quad -144} \\ 3x^2 + -23x + 36 \quad -194 \end{array}$$

$$3x^2 - 23x + 36 + \frac{-194}{x+4}$$

7. Given that the height of a rectangular prism is $x+2$ and the volume is $x^3 - x^2 - 6x$, write an expression that represents the area of the top face of the prism.

$$\begin{array}{r} -2 \overline{) 1 \quad -1 \quad -6 \quad 0} \\ \underline{ 1 \quad -3 \quad 6 \quad 0} \\ 1x^2 - 3x \quad 0 \quad 0 \end{array}$$

$$x^2 - 3x$$

$$(x^2 - 3x)(x + 2)$$

8. Explain the error: Two students used synthetic division to divide $3x^3 - 2x - 8$ by $x - 2$. Determine which solution is correct. Find the error in the other solution.

A.	B.
$\begin{array}{r} 2 \overline{) 3 \quad 0 \quad -2 \quad -8} \\ \underline{ 6 \quad 12 \quad 20} \\ 3 \quad 6 \quad 10 \quad 12 \end{array}$ <p>correct</p>	$\begin{array}{r} 2 \overline{) 3 \quad 0 \quad -2 \quad -8} \\ \underline{ -6 \quad 12 \quad -20} \\ 3 \quad -6 \quad 10 \quad -28 \end{array}$ <p>they multiplied by $\ominus 2$</p>

Review

Graph the function $f(x) = \begin{cases} (x+2)^2, & x < 0 \\ -1, & x > 0 \end{cases}$

